

Given that α and β are in quadrant 4 and $\sin\alpha = -\frac{4}{5}$ and $\cos\beta = \frac{15}{17}$, find:

1. $\cos(\alpha)$

2. $\sin(\beta)$

3. $\sin(\alpha + \beta)$

4. $\cos(\alpha - \beta)$

5. $\cot(\alpha - \beta)$

6. If $\sin\theta = \frac{1}{3}$ and $90^\circ < \theta < 180^\circ$, then find the value of $\sec\theta$

Use sum/difference formulas to find the exact value of the following:

7. $\sin 60^\circ = \sin(90^\circ - 30^\circ)$

8. $\cos 75^\circ = \cos(120^\circ - 45^\circ)$

Write as the sin, cos, or tan of a single angle.

9. $\sin 70^\circ \cos 40^\circ - \cos 70^\circ \sin 40^\circ$

10. $\cos 210^\circ \cos 80^\circ + \sin 210^\circ \sin 80^\circ$

Verify the following.

1. $\sec \theta \cot \theta = \csc \theta$

2. $\sin \theta \csc \theta - \sin^2 \theta = \cos^2 \theta$

3. $\sin(x + y) + \sin(x - y) = 2 \sin x \cos y$

4. $\frac{\csc \theta}{\sec \theta} + \frac{\cos \theta}{\sin \theta} = 2 \cot \theta$

5. $\frac{\sec^2 \theta}{\tan \theta} = \sec \theta \csc \theta$

6. $\cos^2 x(1 + \tan^2 x) = 1$

7. $1 + \sec^2 \theta \sin^2 \theta = \sec^2 \theta$

8. $\frac{1}{1 - \cos x} - \frac{1}{1 + \cos x} = 2 \csc x \cot x$

9. $\frac{\sin^2 \theta + 5 \sin \theta + 6}{\sin^2 \theta - 4} = \frac{\sin \theta + 3}{\sin \theta - 2}$

10. $\sin x(1 - 2 \cos^2 x + \cos^4 x) = \sin^5 x$