

**GSE PreCalculus**  
**Test 5B Review: Trig Identities**

Name \_\_\_\_\_

**Know the following:**

1. Unit Circle – finding the exact value of angle (i.e.  $\cos 60$ )
2. Inverses
  - a. Identify the graphs of inverse functions (sin, cos, tan)
  - b. How to find the inverse given the coordinate (i.e.  $\cos^{-1}\left(\frac{1}{2}\right)$  - answer in degrees and radians)

**Given that  $\alpha$  and  $\beta$  are in quadrant 2 and  $\sin\alpha = \frac{4}{5}$  and  $\cos\beta = -\frac{15}{17}$ , find:**

1.  $\cos\alpha$

2.  $\sin\beta$

3.  $\sin(2\alpha)$

4.  $\cos(2\beta)$

5.  $\tan(2\beta)$

6.  $\cos(\alpha + \beta)$

**Use half angle formulas to solve the following**

7.  $\cos 157.5^\circ =$

8.  $\sin 15^\circ =$

**Solve.**

9.  $2\sin^2 x = 2 + \cos x$

10.  $2\sin\alpha\cos\alpha = \sin\alpha$

11.  $\sin^2 x - 3\cos x = 3$

12.  $2\sin^2 x = 9\sin x + 5$

13.  $\sin^2 \beta - \sin\beta = 0$

**Verify the following.**

14.  $\sin(x + y) + \sin(x - y) = 2\sin x \cos y$

15.  $\frac{\sin x}{\sin x - \cos x} = \frac{1}{1 - \cot x}$

16.  $\sec^4 x - \tan^4 x = 1 + 2\tan^2 x$

16.  $\cos^2 x(1 + \tan^2 x) = 1$

17.  $\csc 2\theta = \frac{\csc \theta}{2\cos \theta}$

18.  $\sec 2\theta = \frac{\sec^2 \theta}{2 - \sec^2 \theta}$

19.  $\cos^4 x - \sin^4 x = \cos 2x$

20.  $(\sin x + \cos x)^2 = 1 + \sin 2x$

**Cumulative Review from Test 1-5A:**

21. Identify the following conics: a.  $\frac{(x-3)^2}{25} + \frac{y^2}{9} = 1$

b.  $(x+1)^2 + y^2 = 16$

22. Multiply the following matrices:  $\begin{bmatrix} x & -1 \\ 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} 3 & 2 \\ -2 & 1 \end{bmatrix}$

23. Solve the linear system:  
 $2x + 4y = 8$   
 $x - 2y = 12$

24. Find a positive co-terminal angle to: a.  $\theta = -\frac{2\pi}{7}$       b.  $\theta = \frac{\pi}{5}$

25. . If  $\tan \theta = \frac{5}{12}$  and  $\theta$  is in quadrant 3, what is the exact value of  $\cos \theta$ ?

26. Find the reference angle: a.  $\theta = 120^\circ$       b.  $\theta = 315^\circ$

27. Find the exact value of the following function:  $\sin\left(-\frac{4\pi}{3}\right)$

28. Evaluate:  $\cos^{-1}\left(\frac{1}{2}\right)$