

Name _____ Date _____

Transformations of Functions

$$f(x) \rightarrow af(x-h)+k$$

What does a do?

- reflect across the x-axis. (-a)
- vertical stretch ($a > 1$)
- vertical shrink ($0 < a < 1$)

What does h do?

- moves left (+h)
- moves right (-h)

What does k do?

- moves up (+k)
- moves down (-k)

Describe the transformations that are applied.

Function	a	h	k
1. $f(x-3)+5$			
2. $-f(x)+3$			
3. $f(x+2)-3$			
4. $\frac{1}{3}f(x)-7$			
5. $-3f(x+1)+5$			

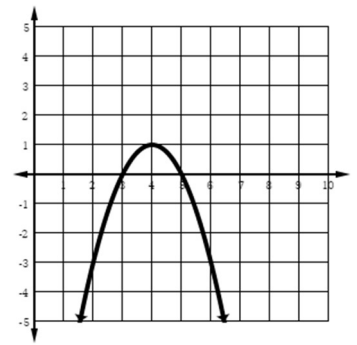
Consider the function: $f(x) = 3x + 2$, and apply the following transformations. Write the new function.

6. $f(x) + 3$
7. $f(x) - 2$
8. shift down 4

Consider the function: $g(x) = (x-2)^2 + 1$, and apply the following transformations. Write the new function.

9. $g(x) + 2$
10. $g(x-2)$
11. reflect over the x-axis and shift down 3
12. shift right 1 and up 3

Given the graph of $f(x)$ on the right, match the following three functions to their graphs.

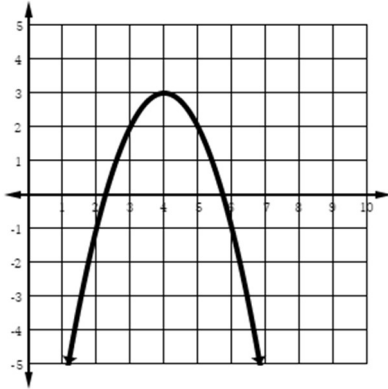


13. $f(x) - 2$

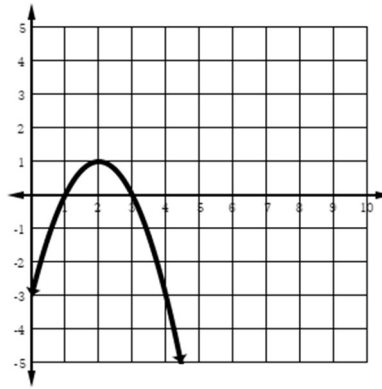
14. $f(x) + 2$

15. $f(x + 2)$

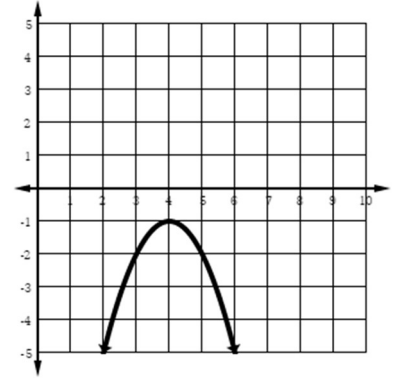
A.



B.



C.



16. Which of the following functions represent a shift right 4 and up 3?

A. $f(x + 4) - 3$

B. $f(x - 4) + 3$

C. $f(x - 4) - 3$

D. $f(x + 4) + 3$

17. Which of the following functions are reflected over the x-axis and shifted left 11?

A. $-f(x) - 11$

B. $-f(x) + 11$

C. $-f(x - 11)$

D. $-f(x + 11)$

18. Which of the following functions have been moved right 3 units?

A. $f(x) - 3$

B. $f(x) + 3$

C. $f(x - 3)$

D. $f(x + 3)$

19. Which of the following functions are reflected over the x-axis, shifted down 8, and left 9?

A. $-f(x - 8) + 9$

B. $-f(x + 9) - 8$

C. $-f(x - 8) - 9$

D. $-f(x - 9) - 8$