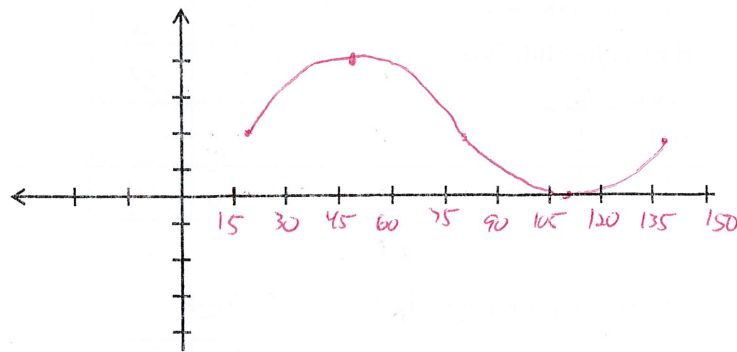


1. $f(x) = 2 \sin(3x - 60^\circ) + 2$

Amplitude: 2
 Period: 120
 Vertical Shift: 2
 Horizontal Shift: 20
 Start: 20
 End: 140
 Increments: 30

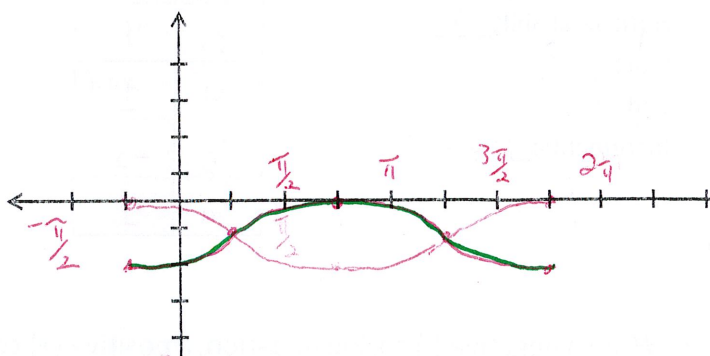
| x | f(x) |
|-----|------|
| 20 | 2 |
| 50 | 4 |
| 80 | 2 |
| 110 | 0 |
| 140 | 2 |



2. $f(x) = -\cos(x + \frac{\pi}{4}) - 1$

Amplitude: 1
 Period: 2π
 Vertical Shift: -1
 Horizontal Shift: -π/4
 Start: -π/4
 End: 7π/4
 Increments: π/2

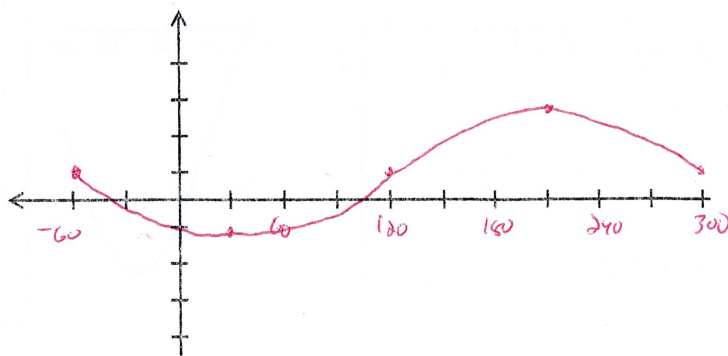
| x | f(x) |
|----------|------|
| $-\pi/4$ | -2 |
| $\pi/4$ | -1 |
| $3\pi/4$ | 0 |
| $5\pi/4$ | -1 |
| $7\pi/4$ | -2 |



3. $f(x) = -2 \sin(x + 60^\circ) + 1$

Amplitude: 2
 Period: 360
 Vertical Shift: 1
 Horizontal Shift: -60
 Start: -60
 End: 300
 Increments: 90

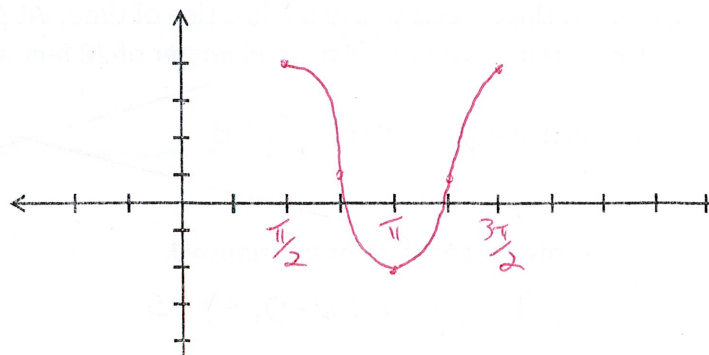
| x | f(x) |
|-----|------|
| -60 | 1 |
| 30 | -1 |
| 120 | 1 |
| 210 | 3 |
| 300 | 1 |



4. $f(x) = 3 \cos(2x - \pi) + 1$

Amplitude: 3
 Period: π
 Vertical Shift: 1
 Horizontal Shift: π/2
 Start: π/2
 End: 3π/2
 Increments: π/4

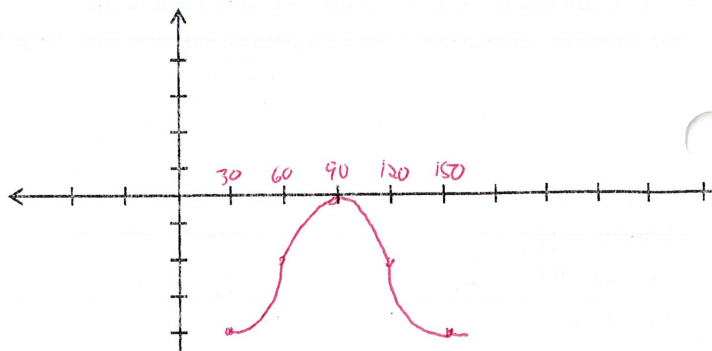
| x | f(x) |
|----------|------|
| $\pi/2$ | 4 |
| $3\pi/4$ | 1 |
| π | -2 |
| $5\pi/4$ | 1 |
| $3\pi/2$ | 4 |



5. $f(x) = -2 \cos(3x - 90^\circ) - 2$

- Amplitude: 2
 Period: 120
 Vertical Shift: -2
 Horizontal Shift: 30
 Start: 30
 End: 150
 Increments: 30

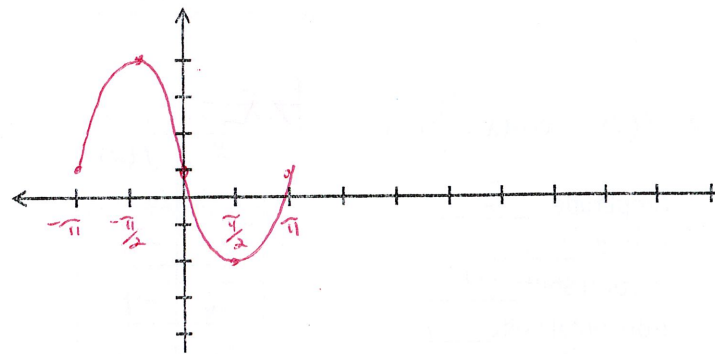
| x | f(x) |
|-----|------|
| 30 | -4 |
| 60 | -2 |
| 90 | 0 |
| 120 | -2 |
| 150 | -4 |



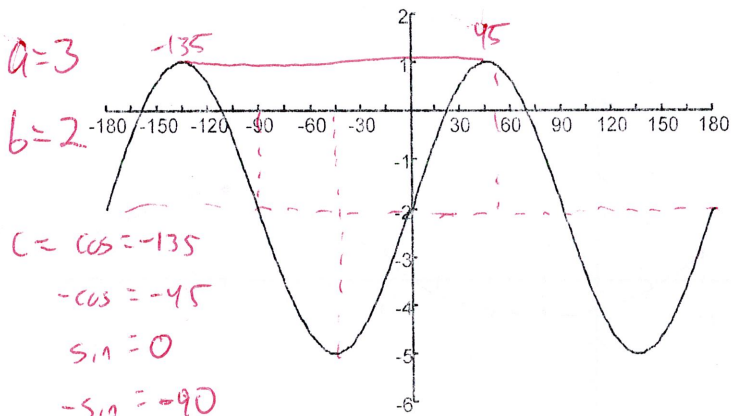
6. $f(x) = 3 \sin(x + \pi) + 1$

- Amplitude: 3
 Period: 2π
 Vertical Shift: 1
 Horizontal Shift: -π
 Start: -π
 End: π
 Increments: π/2

| x | f(x) |
|------|------|
| -π | 1 |
| -π/2 | 4 |
| 0 | 1 |
| π/2 | -2 |
| π | 1 |



7. Write a negative (-) cosine equation, a positive (+) cosine equation, a negative (-) sine equation, and a positive (+) sine equation for the following trig graph



$a=3$

$b=2$

- $c = \cos = -135$
 $-\cos = -45$
 $\sin = 0$
 $-\sin = -90$

$d = -2$

| | |
|----------------|--|
| (-) $\cos x =$ | $-3 \cos(2x + 90) - 2$ or $(2x - 90)$ |
| (+) $\cos x =$ | $3 \cos(2x + 270) - 2$ |
| (-) $\sin x =$ | $-3 \sin(2x + 180) - 2$ |
| (+) $\sin x =$ | $3 \sin(2x) - 2$ |

8. **Steamboat Problem:** A point on a paddlewheel of a boat turns in such a way that its distance, d , from the water's surface was a sinusoidal function of time. At 3 seconds, the point was at its highest, 15 feet above the water's surface. The wheel has a diameter of 20 feet and it completes a revolution once every 10 seconds.

a. Sketch a graph of this sinusoid.

b. Write an equation of the sinusoid.

$F(x) = 10 \sin 36(x - 0.5) + 5$

$F(x) = 10 \cos 36(x - 3) + 5$

$F(x) = -10 \sin 36(x - 5.5) + 5$

$F(x) = -10 \cos 36(x - 8) + 5$

