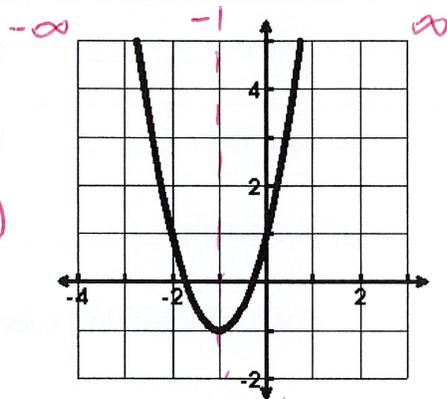


Name: Guide Date: \_\_\_\_\_

**Characteristics of Functions**

1.  $f(x) = 2x^2 + 4x + 1$

- a. Domain:  $(-\infty, \infty)$     b. Range:  $[-1, \infty)$
- c. Extrema:  $\text{Min}(-1, -1)$     d. Zeros:  $x = -0.3, -1.7$
- e. Increasing:  $(-1, \infty)$     f. Decreasing:  $(-\infty, -1)$
- g. End Behavior:  $x \rightarrow \infty, y \rightarrow \infty$

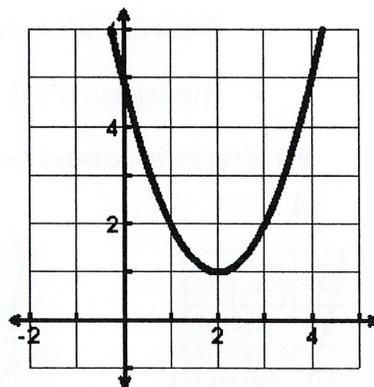


$x \rightarrow -\infty, y \rightarrow \infty$

h. Average rate of change  $[0, 2] \quad \frac{17-1}{2-0} = \frac{16}{2} = 8$

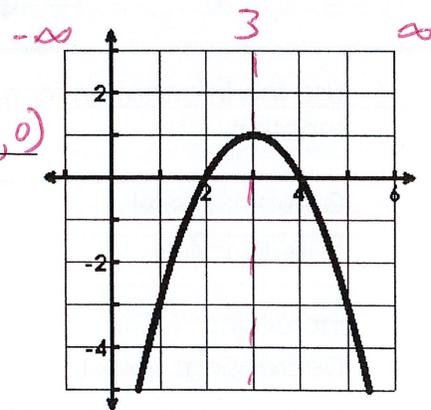
2.  $f(x) = (x-2)^2 + 1$

- a. Range: \_\_\_\_\_    b. Y-intercept: \_\_\_\_\_
- c. Extrema: \_\_\_\_\_    d. Axis of Sym: \_\_\_\_\_
- e. Increasing: \_\_\_\_\_    f. Decreasing: \_\_\_\_\_
- g. Average rate of change  $[0, 2]$  \_\_\_\_\_



3.  $f(x) = -(x-2)(x-4)$

- a. Domain:  $(-\infty, \infty)$     b. Range:  $(-\infty, 1]$
- c. Axis of Sym:  $x = 3$     d. x - intercepts:  $(2, 0), (4, 0)$
- e. Increasing:  $(-\infty, 3)$     f. Decreasing:  $(3, \infty)$
- g. End Behavior:  $x \rightarrow \infty, y \rightarrow -\infty$



$x \rightarrow -\infty, y \rightarrow -\infty$

h. Average rate of change  $[0, 2] \quad \frac{0-(-8)}{2-0} = \frac{8}{2} = 4$

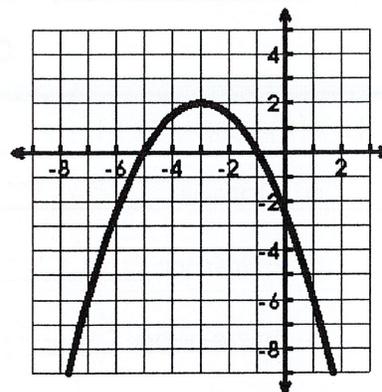
4. This graph represents a quadratic function.

a. Extrema: \_\_\_\_\_ b. Axis of Sym: \_\_\_\_\_

c. Zeros: \_\_\_\_\_ d. y-intercept: \_\_\_\_\_

e. Domain: \_\_\_\_\_ f. Range: \_\_\_\_\_

g. Increasing: \_\_\_\_\_ h. Decreasing: \_\_\_\_\_



i. For the increasing interval, is the rate of change increasing or decreasing?

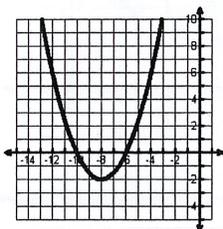
j. For the decreasing interval, is the rate of change increasing or decreasing?

5. The quadratic function  $f(x)$  has these characteristics:

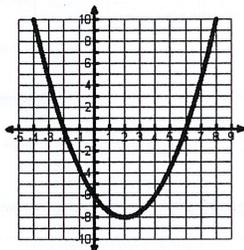
- The vertex is located at  $(8, -2)$ .
- The range is  $[-2, \infty)$ .

Which graph could be  $f(x)$ ?

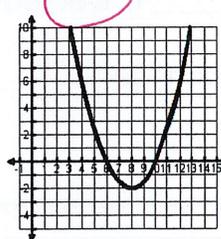
a)



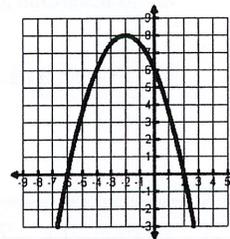
b)



c)



d)



6. Use the information for a given quadratic function to sketch a picture of the function.

Domain:  $(-\infty, \infty)$

Range:  $[-2, \infty)$

Increasing:  $(-1, \infty)$

Decreasing:  $(-\infty, -1)$

There is no stretch or shrink ( $a = 1$ )

