

Unit 2 Test Review

1. Given the following chart, if we add the given points to it, will it remain a function? Say why or why not for each point.

x	-2	0	5	8	13
y	6	-4	9	12	-3

a) (3,9) Yes. 3 isn't a repeated x.

b) (8,7) No. 8 is already there with 12 as y.

c) (13,-3) Yes. This point is already completely in the chart.

2. Solve the given systems by the requested methods:

a) Elimination: $\begin{cases} 16x + 7y = 5 \\ 8x - 3y = -17 \end{cases} \Rightarrow \begin{array}{r} 16x + 7y = 5 \\ 8x - 3y = -17 \\ \hline 16x + 7y = 5 \\ 16x - 6y = -34 \\ \hline 13y = 39 \\ y = 3 \end{array}$

$$16x + 7(3) = 5$$

$$16x + 21 = 5$$

$$16x = -16$$

$$x = -1$$

$$\boxed{(-1, 3)}$$

b) Substitution: $\begin{array}{l} 3x - y = 10 \\ y = 4x - 11 \end{array}$

$$3x - (4x - 11) = 10$$

$$y = 4(1) - 11$$

$$3x - 4x + 11 = 10$$

$$y = 4 - 11$$

$$-x + 11 = 10$$

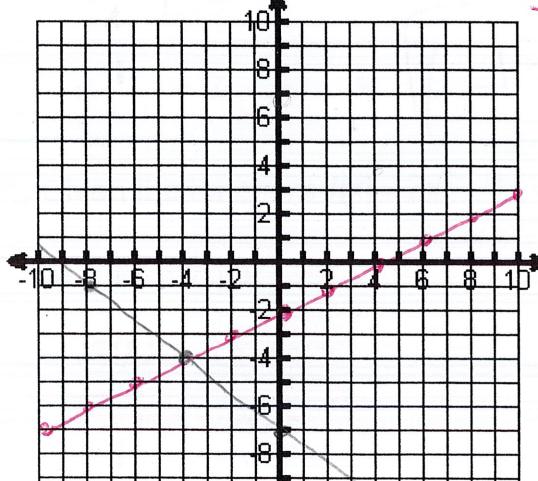
$$y = -7$$

$$-x = -1$$

$$x = 1$$

$$\boxed{(1, -7)}$$

c) Graphing: $\begin{array}{l} x - 2y = 4 \\ 3x + 4y = -28 \end{array}$

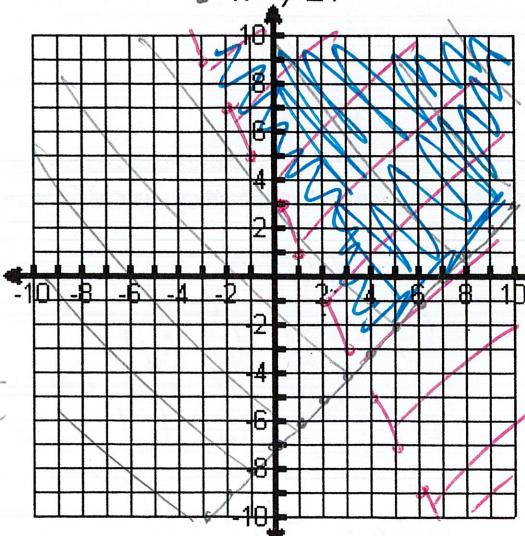


$$\boxed{(-4, -4)}$$

$$\begin{array}{l} x - 2y = 4 \\ -x - 2y = -x \\ -2y = -x + 4 \\ \hline -2 \quad -2 \quad -2 \\ y = \frac{1}{2}x - 2 \end{array}$$

$$\begin{array}{l} 3x + 4y = -28 \\ -3x \quad -3x \\ 4y = -3x - 28 \\ \hline 4 \quad 4 \quad 4 \\ y = -\frac{3}{4}x - 7 \end{array}$$

d) Inequalities: $\begin{array}{l} 2x + y > 3 \\ x - y \leq 7 \end{array}$



$$\begin{array}{l} 2x + y > 3 \\ -x \quad -x \\ y > -2x + 3 \\ 0 > -2(0) + 3 \\ 0 > 3 \\ \text{False} \end{array}$$

$$\begin{array}{l} x - y \leq 7 \\ -y \quad -y \\ x \leq y + 7 \\ 0 \geq 0 - 7 \\ 0 \geq -7 \\ \text{True} \end{array}$$

3. Is $(5, 9)$ a solution to $12 - 4x \geq 24$? Why or why not?

$$12 - 4(5) \geq 24$$

$$12 - 20 \geq 24$$

$$-8 \geq 24$$

No. It results as a false statement when you plug it in.

4. Zion is buying decorations for Homecoming. Balloons cost \$7 a pack and streamers are \$12 a pack. If the decorating budget has \$250, write an inequality for the cost of balloon and streamers that they can buy

$b = \# \text{ of balloons bought}$

$$7b + 12s = 25$$

$s = \# \text{ of streamers bought}$

$$7b + 12s \leq 250$$

5. You are on a farm that raises cows and chickens. If there are 20 animals total, and the animals have 56 legs in total (assume a standard number of legs for the animals), how many cows and how many chickens are there?

$m = \# \text{ of cows}$

$$\begin{aligned} 4m + 2c &= 56 \\ 2(m + c) &= 20 \end{aligned} \Rightarrow \begin{aligned} 4m + 2c &= 56 \\ 2m + 2c &= 40 \\ 2m &= 16 \end{aligned} \quad \begin{aligned} m + c &= 20 \\ 8 + c &= 20 \\ c &= 12 \end{aligned}$$

$c = \# \text{ of chickens}$

There are 8 cows and 12 chickens $m = 8$

6. Solve the following equations for the requested variables:

a) $r = fh + c; h$

$$\frac{-c}{f} \quad \frac{-c}{f}$$

$$\frac{r-c}{f} = h$$

b) $P = 2(L + W); L$

$$\frac{P}{2} \quad \frac{P}{2}$$

$$\frac{P}{2} = L + W$$

$$-\cancel{W} \quad -\cancel{W}$$

$$\frac{P}{2} - W = L$$

7. Find a_n for the arithmetic sequence $7, 3, -1, \dots$

$$a_n = a_1 + d(n-1)$$

$$a_n = 7 + 4(n-1)$$

$$a_n = 7 - 4n + 4$$

$$\boxed{a_n = -4n + 11}$$

8. $f(x) = \frac{2}{3}x - 4$

a. Domain: $(-\infty, \infty)$ b. Range: $(-\infty, \infty)$

c. Increasing or decreasing? Increasing

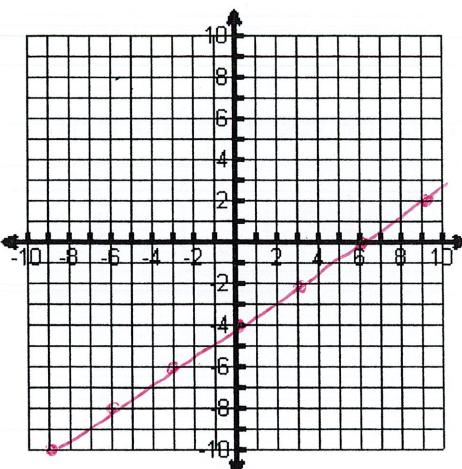
d. x-intercept: $(6, 0)$ e. y-intercept: $(0, -4)$

$$x \rightarrow -\infty \quad f(x) \rightarrow -\infty$$

e. End Behavior:

$$x \rightarrow \infty \quad f(x) \rightarrow \infty$$

f. Rate of change from $[-3, 6]$ $\frac{0 - (-6)}{6 - (-3)} = \frac{6}{9} = \frac{2}{3}$



\uparrow Hey, that's the slope!

9. What is the 10th term in an arithmetic sequence whose third term is 17 and whose common difference is 8?

$$d=8 \quad \begin{array}{c} 3 \\ \nearrow \\ -8 \end{array} \quad \begin{array}{c} 11 \\ \nearrow \\ -8 \end{array} \quad \begin{array}{c} 17 \\ \nearrow \\ -8 \end{array}$$

$$a_1 = 3$$

$$a_n = a_1 + d(n-1)$$

$$a_{10} = 3 + 8(10-1)$$

$$a_{10} = 3 + 8(9)$$

$$a_{10} = 3 + 72$$

$$a_{10} = 75$$

10. Convert the following sequences between explicit and recursive:

a) $a_n = 7n - 11$

b) $a_n = a_{n-1} - 4; a_1 = 6$

$$d=7$$

$$a_1 = 7(1) - 11 = 4$$

$$\boxed{a_n = a_{n-1} + 7; a_1 = 4}$$

$$d = -4 \quad a_n = a_1 + d(n-1)$$

$$a_1 = 6 \quad a_n = 6 + 4(n-1)$$

$$a_n = 6 + 4n - 4$$

$$\boxed{a_n = -4n + 10}$$

11. Given the functions $f(x) = 3x^2 - 4x + 19$ and $g(x) = 6x + 35$

a) $g(8) = 6(8) + 35$

$$g(8) = 48 + 35$$

$$\boxed{g(8) = 83}$$

b) $f(-4) = 3(-4)^2 - 4(-4) + 19$

$$f(-4) = 3(16) + 4(-4) + 19$$

$$f(-4) = 48 + 16 + 19$$

$$\boxed{f(-4) = 83}$$